

Markscheme

May 2025

**Mathematics: applications and
interpretation**

Higher level

Paper 2

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Instructions to Examiners

Abbreviations

- M** Marks awarded for attempting to use a correct **Method**.
- A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- R** Marks awarded for clear **Reasoning**.
- AG** Answer given in the question and so no marks are awarded.
- FT** Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

Using the markscheme

1 General

Award marks using the annotations as noted in the markscheme *eg M1, A2*.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award **M0** followed by **A1**, as **A** mark(s) depend on the preceding **M** mark(s), if any.
- Where **M** and **A** marks are noted on the same line, *e.g. M1A1*, this usually means **M1** for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and **A1** for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies **A3, M2** etc., do **not** split the marks, unless there is a note.
- The response to a “show that” question does not need to restate the **AG** line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this working is incorrect and/or suggests a misunderstanding of the question. This will encourage a uniform approach to marking, with less examiner discretion. Although some candidates may be advantaged for that specific question item, it is likely that these candidates will lose marks elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used **in a subsequent part**. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award **FT** marks as appropriate but do not award the final **A1** in the first part.

Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	No. Last part in question.	Award A1 for the final mark (condone the incorrect further working)
2.	$\frac{35}{72}$	0.468111... (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award A0 for the final mark (and full FT is available in subsequent parts)

3 Implied marks

Implied marks appear in **brackets e.g. (M1)**, and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

4 Follow through marks (only applied after an error is made)

Follow through (**FT**) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award **FT** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then **FT** marks should be awarded for *their* correct answer, even when working is not present.

For example: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is **(M1)A1**, it is possible to award full marks for *their* correct answer, **without working being seen**. For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** marks may be awarded if appropriate.
- If the question becomes much simpler because of an error then use discretion to award fewer **FT** marks, by reflecting on what each mark is for and how that maps to the simplified version.
- If the error leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word “their” in a description, to indicate that candidates may be using an incorrect value.
- If the candidate’s answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any **FT** marks in the subsequent parts. This includes when candidates fail to complete a “show that” question correctly, and then in subsequent parts use their incorrect answer rather than the given value.
- Exceptions to these **FT** rules will be explicitly noted on the markscheme.
- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was “Hence”.

5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (**MR**). A candidate should be penalized only once for a particular misread. Use the **MR** stamp to indicate that this has been a misread and do not award the first mark, even if this is an **M** mark, but award all others as appropriate.

- If the question becomes much simpler because of the **MR**, then use discretion to award fewer marks.
- If the **MR** leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.
- If a candidate uses a correct answer, to a "show that" question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.
- **MR** can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is 'Hence' and not 'Hence or otherwise' then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, etc.
- Alternative solutions for parts of questions are indicated by **EITHER . . . OR**.

7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and 1,9 or 1000 and 1,000 and 1.000.
- Do not accept final answers written using calculator notation. However, **M** marks and intermediate **A** marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, some **equivalent** answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.*

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come “*from the use of 3 sf values*”.

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an **A** mark to be awarded, arithmetic should be completed, and any values that lead to integers should be simplified; for example, $\sqrt{\frac{25}{4}}$ should be written as $\frac{5}{2}$. An exception to this is simplifying fractions, where lowest form is not required (although the numerator and the denominator must be integers); for example, $\frac{10}{4}$ may be left in this form or written as $\frac{5}{2}$.

However, $\frac{10}{5}$ should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g. $4e^{2x} \times e^{3x}$ should be simplified to $4e^{5x}$, and $4e^{2x} \times e^{3x} - e^{4x} \times e^x$ should be simplified to $3e^{5x}$. Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so $x(x+1)$ and $x^2 + x$ are both acceptable.

Please note: intermediate **A** marks do NOT need to be simplified.

9 Calculators

A GDC is required for this paper, but if you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

10. Presentation of candidate work

Crossed out work: If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

More than one solution: Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is “first”.

Q1.

(a) $(d =) 3l$ **A1**

[1 mark]

(b) substitution into volume of cuboid formula $V = l^2 \times 3l (= 375)$ **(M1)**

attempting to solve their $3l^3 = 375$ **(M1)**

$$l^3 = 125 \text{ OR } l = \sqrt[3]{125} \text{ OR } l^3 = \frac{375}{3}$$

$l = 5, d = 15$ **A1**

[3 marks]

(c) finding the area of a square and the area of a (non-square) rectangle 5×5 and 5×15 **(M1)**

$$(5 \times 5 + 5 \times 15 + 5 \times 15) \times 2 \quad \text{A1}$$

$$= 350\text{cm}^2 \quad \text{A1}$$

Note: The final answer is 350cm^2 . Units are required.

[3 marks]

(d) $\pi r^2 h = 375$ **(A1)**

$$h = \frac{375}{\pi r^2} \quad \text{A1}$$

Note: Award at most **A0A1** for a final answer $h = \frac{V}{\pi r^2}$.

[2 marks]

(e) attempt to substitute their h into the curved surface area $2\pi r h$ **M1**

$$A = 2\pi r^2 + 2\pi r \left(\frac{375}{\pi r^2} \right) \quad \text{A1}$$

$$A = 2\pi r^2 + \frac{750}{r} \quad \text{AG}$$

[2 marks]

(f) $\left(\frac{dA}{dr} = \right) 4\pi r - 750r^{-2}$ **A1A1A1**

Note: Award **A1** for $4\pi r$, **A1** for -750 , **A1** for r^{-2} or equivalent. Award at most **A1A1A0** for additional terms seen.

[3 marks]

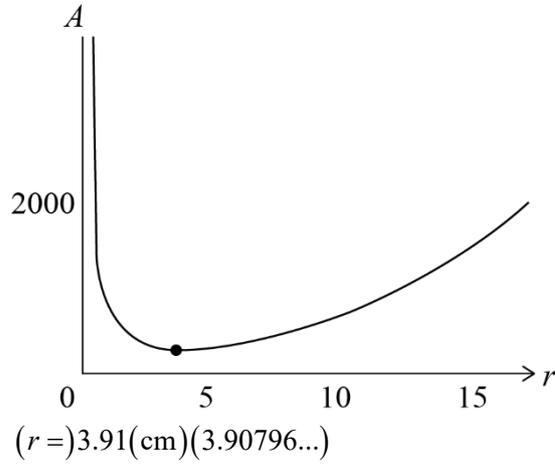
continued...

Question 1 continued.

(g) (i)

METHOD 1

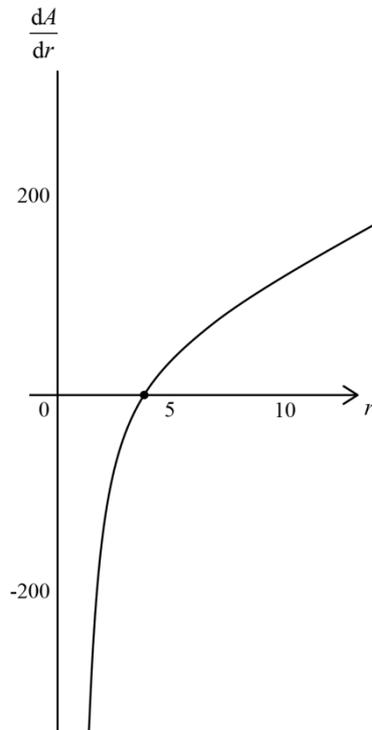
correct sketch with some indication of min point (need not be labelled) **(M1)**



A1

METHOD 2

attempt to solve $4\pi r - \frac{750}{r^2} = 0$, graphically or otherwise **(M1)**



$(r =) 3.91(\text{cm})(3.90796\dots)$

A1

(ii) $288(\text{cm}^2)(287.873\dots)$

A1

[3 marks]

continued...

Question 1 continued.

(h) (i) $\left(\frac{d^2A}{dr^2}\right) = 4\pi + \frac{1500}{r^3}$ **A1**

(ii) (as $r > 0$), $\frac{d^2A}{dr^2} > 0$ **R1**

hence graph is concave-up. **A1**

Note: Do not award R0A1 . Marks can only be awarded in part (ii) if an expression is seen in part (i).
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[3 marks]

Total [20 marks]

Q2.

(a)	$\frac{360}{12}$	M1
	$= 30$	AG

Note: Award **M0** for use of given value, 30.

(b)	substitution of $t = 5$ into model $(-2.5 \cos(30 \times 5) + 4.5)$	[1 mark] (M1)
	$h(5) = 6.67(6.66506\dots)$	A1

Note: Award **M1A0** for 2.75187... (radian answer).

(c)	(i)	2.5 (m)	[2 marks] A1
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Note: Award **A0** for -2.5 (m)

(ii)	$h(t) = 4.5$	A1A1
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Note: Award **A1** for an equation of a horizontal line $h = \text{constant}$ (accept $y = \text{constant}$), **A1** for that constant being 4.5. Second **A1** is dependent on first **A1**. Do not award **A0A1**.

[3 marks]

(d)	attempt at finding point of intersection between $h(t) = \text{constant}$ and the curve using $h(t) = 2.55$ or $h(t) + 0.1 = 2.65$ to find intersection	(M1) (A1)
	13.3 (13.2913...)	(A1)
	13:17 (1:17 p.m.)	A1

Note: The final **A1** can be awarded for correctly converting **their** value of t into a time.

[4 marks]

continued...

Question 2 continued.

- (e) using $h(t) = 2.75$ or $h(t) - 0.1 = 2.65$ to find intersection (A1)
22.4809... – 13.2913... – 0.5 (A1)(M1)(M1)

Note: Award **A1** for 22.4809... seen, **M1** for subtracting their two times for harbour, **M1** for subtracting 0.5 from their answer at any stage of the work.

8.69 (hours) (8.68958... (hours)) A1

Note: Accept minutes used in working, but the final answer must be in hours.

[5 marks]
Total [15 marks]

Q3.

(a) attempt to substitute into trapezoidal formula **(M1)**

$$(\text{area of cross-section}) \approx \frac{1.9}{2}(0 + 0 + 2(1.68 + 2.81 + 2.32)) \quad \textbf{(A1)}$$

$$= 12.9 \text{ (m}^2\text{)}(12.939) \quad \textbf{A1}$$

[3 marks]

(b) attempt to find the volume of water in one second, their (a) $\times 0.3$ **(M1)**

$$12.939 \times 0.3$$

$$= 3.88(3.8817) \text{ (m}^3\text{)} \quad \textbf{A1}$$

Note: Accept 3.87 for use of 3sf answer to part (a) 12.9.

[2 marks]

(c) $(2.81 - 1.6 =) 1.21 \text{ (m)}$ **A1**

[1 mark]

(d) attempt to find maximum eg graphically or $\frac{dy}{dx} = 0$ or using height at $x = 3.8$ **(M1)**

$$3.07 \text{ (m) OR } 3.066 \text{ (m)} \quad \textbf{A1}$$

Note: Award **M1A0** for coordinate pair (3.8, 3.066)

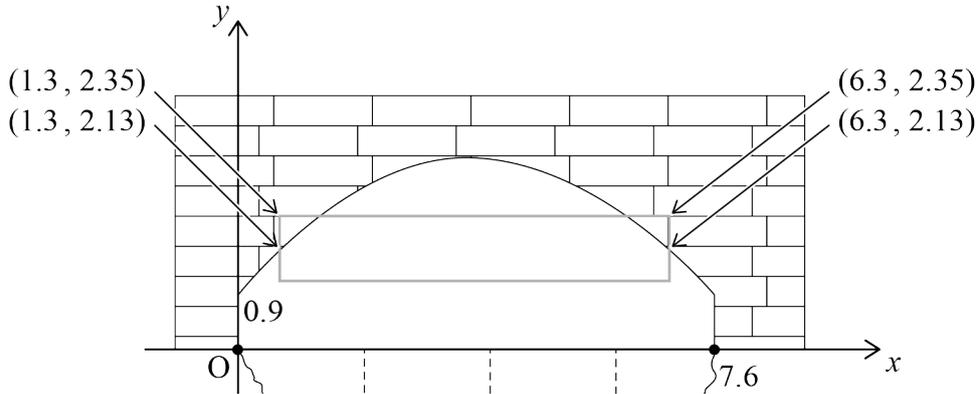
[2 marks]

continued...

Question 3 continued.

(e) **METHOD 1**

height of bridge < height of boat at
 $x = 1.3$ or $x = 6.3$ (5 m wide boat)



use of $3.8 + 2.5$ or $3.8 - 2.5$

(M1)

attempt to find the height of the bridge at either 1.3 or 6.3 m

(M1)

2.13(m)(2.1285)

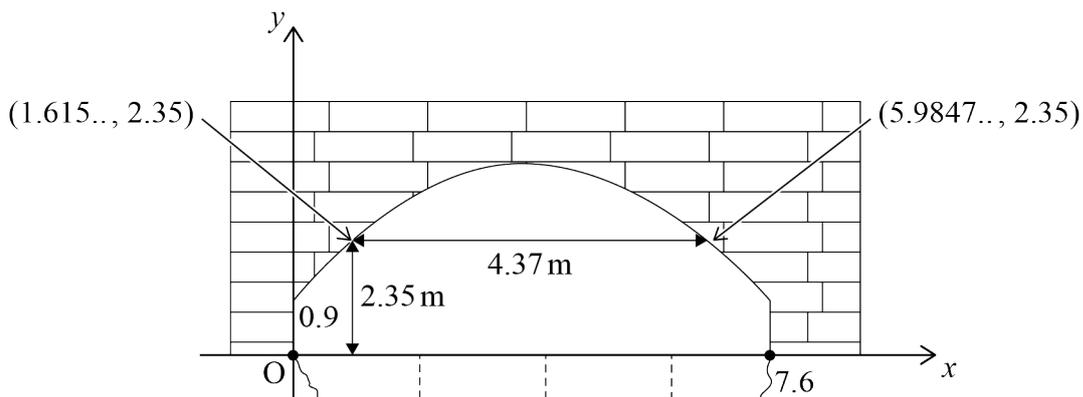
A1

($2.13 < 2.35$) the boat cannot pass under the bridge

A1

METHOD 2

boat is wider (5 m) than the width between
the arch at $h = 2.35$ m (height of boat)



attempt to find the values of x (1.61520... and 5.98479...) when the bridge is
2.35 m above the water

(M1)

continued.

Question 3 continued.

subtract their two values to find the width of bridge at that point at this height (M1)

$5.984795\dots - 1.615204\dots$ OR $3.8 - 1.615204\dots$ OR $5.98479\dots - 3.8$

$4.37(4.36959\dots)(\text{m})$ OR $2.18 (2.18479\dots)(\text{m})$ A1

$(4.37 < 5)$ OR $(2.18 < 2.5)$ the boat cannot pass under the bridge A1

METHOD 3 (see the diagram for method 2)

use of $3.8 + 2.5 (6.3)$ or $3.8 - 2.5 (1.3)$ (M1)

attempt to find the values of x when the bridge is 2.35 m above the water (M1)

$5.98479\dots$ or $1.61520\dots (\text{m})$ A1

$6.3 > 5.98\dots(5.98479\dots)$ or $1.3 < 1.62 (1.61520\dots)$ the boat cannot pass under the bridge A1

Note: In all 3 methods the final **A1** is dependent on the previous **A1**.

[4 marks]

[Total 12 marks]

Q4. (a) between A and E **A1**
[1 mark]

(b) (i) attempt to find M^3 **M1**

$$M^3 = \begin{pmatrix} 1 & 3 & 1 & 1 & 3 \\ 3 & 1 & 3 & 1 & 4 \\ 0 & 3 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 2 \\ 0 & 4 & 0 & 2 & 1 \end{pmatrix}$$

contains 0 so some routes are not possible **R1**

Note: Identification of any route which is not possible, award **R1**, provided **M1** has been awarded.

(ii) **METHOD 1**
attempt to find $M + M^2 + M^3$ OR $M^2 + M^3$ **M1**

$$M + M^2 + M^3 = \begin{pmatrix} 2 & 5 & 2 & 2 & 5 \\ 4 & 4 & 4 & 2 & 6 \\ 1 & 4 & 1 & 1 & 2 \\ 1 & 1 & 1 & 1 & 3 \\ 1 & 5 & 1 & 3 & 3 \end{pmatrix}, M^2 + M^3 = \begin{pmatrix} 2 & 4 & 2 & 2 & 4 \\ 3 & 4 & 3 & 2 & 5 \\ 1 & 3 & 1 & 1 & 2 \\ 1 & 1 & 1 & 1 & 2 \\ 1 & 4 & 1 & 2 & 3 \end{pmatrix}$$

all ports can be reached in 3 trips or fewer, **A1**

because there are no 0 entries **R1**

Note: The complete matrix does not need to be seen for **M1** to be awarded. **A1** and **R1** are dependent on the **M1**.

continued...

Question 4 continued.

METHOD 2

attempt to find M^2

M1

$$M^2 = \begin{pmatrix} 1 & 1 & 1 & 1 & 1 \\ 0 & 3 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 2 \end{pmatrix}$$

all ports can be reached in 3 trips or fewer,

A1

because there are no overlapping 0 entries in M^2 and M^3

R1

Note: The complete matrix does not need to be seen for **M1** to be awarded. **A1** and **R1** are dependent on the **M1**.

[5 marks]

(c) attempt to find the cost of a route of length 2

M1

route CAD has cost $7 + 8 = 15$

route CBD has cost $4 + 9 = 13$

route CED has cost $10 + 3 = 13$

A1A1

Note: Award **A1** for at least one correct answer, **A1** for all three correct answers.
Accept CBED has cost $4 + 6 + 3 = 13$ in place of CBD and CED

hence least cost is 13 euros

AG

[3 marks]

continued...

Question 4 continued.

- (d) evidence of correct algorithm used, ABC... seen, or in a diagram (M1)
ABCEDA OR $3 + 4 + 10 + 3 + 8$ A1
cost 28 euros A1
[3 marks]

- (e) evidence of selecting three edges not including vertex A (M1)
length of spanning tree = $4 + 6 + 3 (= 13)$ (A1)
reconnect vertex A using two distinct edges (M1)
lower bound ($13 + 3 + 5 =$)21 A1
[4 marks]

[Total 16 marks]

Q5. (a) (2, 1, 0)

A1

Note: Condone coordinates written as a vector.

[1 mark]

(b) (i) $5 \begin{pmatrix} -4 \\ 4 \\ 7 \end{pmatrix}$ or $\begin{pmatrix} -18 \\ 21 \\ 35 \end{pmatrix} - \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}$

(M1)

Note: Condone one error in the position vector for B for **M1**

$$\begin{pmatrix} -20 \\ 20 \\ 35 \end{pmatrix}$$

A1□

(ii) use of formula for magnitude with their \vec{AB}

(M1)

$$\sqrt{(-20)^2 + 20^2 + (35)^2}$$

45 (m)

A1

Note: Do not accept $\sqrt{2025}$.

[4 marks]

(c) **METHOD 1**

use of two direction vectors

(M1)

use of formula for scalar product

(M1)

$$\begin{pmatrix} -4 \\ 4 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix} = 12 \quad (\text{OR equivalent multiple of 12})$$

(A1)

$$\cos(\hat{CAB}) = \frac{12}{\sqrt{81}\sqrt{5}}$$

(A1)

$$\hat{CAB} = 53.4^\circ (53.3957\dots^\circ, 0.932, 0.931931\dots)$$

A1

continued...

Question 5 continued.

METHOD 2

attempt to find a point C using $\begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix}$ or some value of λ **(M1)**

eg $C = (1, 3, 0)$

$|\vec{AC}| = \sqrt{5}$, $|\vec{BC}| = 43.7 (= \sqrt{1910})$ OR equivalent **(A1)**

attempt to use the cosine rule **(M1)**

$\cos(\hat{CAB}) = \frac{5 + 45^2 - 1910}{2 \times \sqrt{5} \times 45}$ OR equivalent **(A1)**

$\hat{CAB} = 53.4^\circ (53.3957\dots^\circ, 0.932, 0.931931\dots)$ **A1**

[5 marks]

(d) let P_2 be at the point D when $t = 5$

EITHER

use of distance = speed \times time **(M1)**

distance travelled by $P_2 = 12 \times 5$

= 60 **(A1)**

use of cosine rule **(M1)**

$\left(|\vec{BD}|^2 = \right) 45^2 + 60^2 - 2 \times 45 \times 60 \cos(53.3957\dots) (= 2405.06\dots)$ **(A1)**

continued...

Question 5 continued.

OR

position of P_1 $\begin{pmatrix} -18 \\ 21 \\ 35 \end{pmatrix}$ **(A1)**

position of P_2

attempt to calculate $r = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} + \lambda \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix}$ for any value of λ **(M1)**

$r = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} + 5 \times \frac{12}{\sqrt{5}} \begin{pmatrix} -1 \\ 2 \\ 0 \end{pmatrix} \left(= \begin{pmatrix} -24.8328... \\ 54.6656... \\ 0 \end{pmatrix} \right)$ **(A1)**

subtracting their position vectors for P_1 and P_2 **(M1)**

$\vec{BD} = \begin{pmatrix} -24.8328... \\ 54.6656... \\ 0 \end{pmatrix} - \begin{pmatrix} -18 \\ 21 \\ 35 \end{pmatrix}$

THEN

$|\vec{BD}| = 49.0(49.0414...) \text{ (m)}$ **A1**

[5 marks]

Total [15 marks]

- Q6.** (a) (i) 0.45 **A1**
- (ii) attempt to find the expected value (at least two correct products) **(M1)**
 $0 \times 0.21 + 1 \times 0.34 + 2 \times 0.28 + 3 \times 0.17$
 1.41 (customers) **A1**
- [3 marks]**
- (b) $E(T) = 115$ **(A1)**
 1.41×115
 162 (162.15) (seconds) (2 minutes 42 seconds) **A1**
- [2 marks]**
- (c) $P(T > 180)$ **(M1)**
 0.0101(0.0101318...) **A1**

Note: Award **M1A0** for an answer of 0.467.

- [2 marks]**
- (d) attempt at linear combination of two normal variables **(M1)**
 time to serve two people, $T_2 \sim N(230, 2 \times 28^2)$ **(A1)(A1)**
 $P(T_2 > 180) = 0.897$ (0.896649...) **A1**
- [4 marks]**
- (e) (i) (if no-one in the queue the waiting time is 0)
 $(0.21 \times 0) + 0.34 \times 0.0101318... + 0.28 \times 0.896649 + 0.17 \times 1$ **(M1)(A1)**
 0.425 (0.424506...) **A1**
- (ii) $(0.425 > 0.4)$ employ more staff **A1**

Note: Award if consistent with their probability from part (e) (i).

[4 marks]
[Total 15 marks]

- Q7.** (a) argument is 1.31 $(\frac{5\pi}{12}, 1.30899\dots)$ **(A1)**
 modulus is 5 **(A1)**
 $5e^{1.31i}$ $(5e^{\frac{5\pi i}{12}})$ **A1**

Note: Award **A1A1A0** for correct answer $1.29409\dots + 4.82962\dots i$ in incorrect form

[3 marks]

- (b) (i) length of branches in next iteration = 0.7×5 **(M1)**
 $2 \times 5 + 4(0.7 \times 5)$ **A1**
 $= 24$ **AG**

Note: Award **M1A0** for $2 \times 5i + 4(0.7 \times 5i)$.

- (ii) **EITHER**
 recognition of a geometric sequence / series: for example a value given for r , or consideration of the lengths of branches added. **(M1)**
 $r = 2 \times 0.7 (= 1.4)$ **(A1)**
 use of formula for geometric series for 10 terms **(M1)**

$$\frac{10((0.7 \times 2)^{10} - 1)}{0.7 \times 2 - 1}$$
 (A1)
OR
 attempt to find the formula for n^{th} term, for example correct first three terms found
 $2 \times 5 + 2^2 \times 5 \times 0.7 + 2^3 \times 5 \times 0.7^2 + \dots$ **(M1)**
 n^{th} term = $5 \times 0.7^{n-1} \times 2^n$ **(A1)**
 attempt to find a summation for 10 terms clearly shown **(M1)**

$$\sum_{n=1}^{10} 5 \times 0.7^{n-1} \times 2^n$$
 (A1)
THEN
 $= 698(698.136\dots)$ **A1**

continued.

Question 7 continued.

- (iii) **EITHER**
 as common ratio of the geometric series = 1.4 (> 1) **R1**
- OR**
 as the **total** length added at each stage is increasing **R1**
- THEN**
 there is no limit **A1**

Note: Do not award **R0A1**.

[9 marks]

- (c) (i) correct moduli 5, 5×0.7 , 5×0.7^2 (5, 3.5, 2.45) **A1**
- attempt to calculate the argument by adding or subtracting $\frac{\pi}{12}$ (0.261799...)(**M1**)
- correct arguments 1.31, 1.05, 1.31 $\left(\frac{5\pi}{12}, \frac{4\pi}{12}, \frac{5\pi}{12} \right)$ **A1**
- $b = 5e^{1.31i} + 3.5 \times e^{1.05i} + 2.45 \times e^{1.31i} \left(= 5e^{\frac{5\pi}{12}i} + 3.5 \times e^{\frac{\pi}{3}i} + 2.45 \times e^{\frac{5\pi}{12}i} \right)$ **A1**
- (ii) $(b =) 3.68 + 10.2i(3.67820\dots + 10.2272\dots i)$ **A1**

Note: Accept $3.66 + 10.2i$ (from using their 3 sf values).

[5 marks]

Total [17 marks]