2225 – 7319M

Diploma Programme
Programme du diplôme
Programa del Diploma

Markscheme

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Mathematics: applications and interpretation

Standard level

Paper 1

19 pages

Instructions to Examiners

Abbreviations

M Marks awarded for attempting to use a correct **Method**.

A Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding ***M*** marks.

R Marks awarded for clear **Reasoning**.

AG Answer given in the question and so no marks are awarded.

FT Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

Using the markscheme

1 General

Award marks using the annotations as noted in the markscheme *eg **M1**, **A2**.*

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award ***M0*** followed by ***A1***, as ***A*** mark(s) depend on the preceding ***M*** mark(s), if any.
- Where ***M*** and ***A*** marks are noted on the same line, *e.g.* ***M1A1***, this usually means ***M1*** for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and ***A1*** for using the **correct** values.
- Where there are two or more ***A*** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award ***A0A1A1***.
- Where the markscheme specifies ***A3***, ***M2*** *etc*., do **not** split the marks, unless there is a note.
- The response to a "show that" question does not need to restate the ***AG*** line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this working is incorrect and/or suggests a misunderstanding of the question. This will encourage a uniform approach to marking, with less examiner discretion. Although some candidates may be advantaged for that specific question item, it is likely that these candidates will lose marks elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used **in a subsequent part**. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award ***FT*** marks as appropriate but do not award the final ***A1*** in the first part.

Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685... *(incorrect decimal value)*	No. Last part in question.	Award ***A1*** for the final mark *(condone the incorrect further working)*
2.	$\frac{35}{72}$	0.468111… (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award ***A0*** for the final mark *(and full **FT** is available in subsequent parts)*

3 Implied marks

Implied marks appear in **brackets e.g.** ***(M1)***,and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

4 Follow through marks (only applied after an error is made)

Follow through (***FT***) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award ***FT*** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then ***FT*** marks should be awarded for *their* correct answer, even when working is not present.

For example: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is ***(M1)A1***, it is possible to award full marks for *their* correct answer, **without working being seen.** For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further ***A*** marks can be awarded for work which uses the error, but ***M*** marks may be awarded if appropriate.

- If the question becomes much simpler because of an error then use discretion to award fewer ***FT*** marks, by reflecting on what each mark is for and how that maps to the simplified version.

- If the error leads to an inappropriate value (*e.g.* probability greater than 1, $\sin\theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).

- The markscheme may use the word “their” in a description, to indicate that candidates may be using an incorrect value.

- If the candidate’s answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any ***FT*** marks in the subsequent parts. This includes when candidates fail to complete a “show that” question correctly, and then in subsequent parts use their incorrect answer rather than the given value.

- Exceptions to these ***FT*** rules will be explicitly noted on the markscheme.

- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was “Hence”.

5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (***MR***). A candidate should be penalized only once for a particular misread. Use the ***MR*** stamp to indicate that this has been a misread and do not award the first mark, even if this is an ***M*** mark, but award all others as appropriate.

- If the question becomes much simpler because of the ***MR***, then use discretion to award fewer marks.
- If the ***MR*** leads to an inappropriate value (*e.g.* probability greater than 1, $\sin\theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.
- If a candidate uses a correct answer, to a "show that" question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.
- ***MR*** can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is 'Hence' and not 'Hence or otherwise' then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, *etc*.
- Alternative solutions for parts of questions are indicated by **EITHER** . . . **OR**.

7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and 1,9 or 1000 and 1,000 and 1.000.
- Do not accept final answers written using calculator notation. However, ***M*** marks and intermediate ***A*** marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, some **equivalent** answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.*

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come "*from the use of 3 sf values*".

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an ***A*** mark to be awarded, arithmetic should be completed, and any values that lead to integers should be simplified; for example, $\sqrt{\frac{25}{4}}$ should be written as $\frac{5}{2}$. An exception to this is simplifying fractions, where lowest form is not required (although the numerator and the denominator must be integers); for example, $\frac{10}{4}$ may be left in this form or written as $\frac{5}{2}$. However, $\frac{10}{5}$ should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g. $4e^{2x} \times e^{3x}$ should be simplified to $4e^{5x}$, and $4e^{2x} \times e^{3x} - e^{4x} \times e^{x}$ should be simplified to $3e^{5x}$. Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so $x(x+1)$ and $x^2 + x$ are both acceptable.

Please note: intermediate ***A*** marks do NOT need to be simplified.

9 Calculators

A GDC is required for this paper, but if you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

10. Presentation of candidate work

Crossed out work: If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

More than one solution: Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is "first".

Q1.

(a) attempt to substitute coordinates A and C in the formula for midpoint in 3D ***(M1)***

$\left(\frac{-2+1}{2}, \frac{0+3}{2}, \frac{0+0}{2}\right)$

$(-0.5, 1.5, 0)$ OR $\left(-\frac{1}{2}, \frac{3}{2}, 0\right)$ ***A1***

Note*:* Award at most ***M1A0*** for answers not given as coordinates. Accept $x = -0.5, y = 1.5, z = 0$.

[2 marks]

(b) 5 (cm) ***A1***

[1 mark]

(c) attempt to substitute coordinates C and H in the formula for distance between two points in 3D ***(M1)***

$\sqrt{(1-(-0.5))^2 + (3-(1.5))^2 + (0-(5))^2}$

5.43 (5.43139…) (cm) ***A1***

Note: If use of 2D has been penalized in part (a), do not penalize in part (c)

[2 marks]

Total [5 marks]

Q2.

(a) (i) attempt to find mid-values $600, 800, 1000...$ or to substitute in the mean formula

(M1)

$$\frac{600\times 38+800\times 45+1000\times 25+...1600\times 8}{150}$$

937 (kWh) $(937.333\ldots)$ ***A2***

Note: Award at most ***(M1)M1A0*** for an incorrect answer but evidence of correct use of mean formula. Award ***(M1)A0*** for an unsupported 1100 , use of the mid-values can be inferred.

(ii) 299 (kWh) $(299.454\ldots)$ ***A1***

Note: Accept 299.5. If no mark has been awarded in part (a)(i), award A2 for a correct answer seen in part (a)(ii).

[4 marks]

(b) the monthly energy consumption in *Eureka* is less spread out than that of *Helvetia* (or equivalent) ***R1***

Note: Do not accept eg standard deviation in Helvetia is 3 times that in Eureka or interpretations referring to lower average, efficiency, or lower consumption unless clearly related to spread. Some mention of spread is required for the ***R1*** e.g less variation, more consistent, closer together, smaller range, tighter clustering.

[1 mark]

Total [5 marks]

Q3.

(a) attempt to substitute 0.5 into function ***(M1)***

$h(0.5)=\dfrac{20}{2\times 0.5+5}$

$3.33\ (\text{m})\ (3.33333\ldots,\dfrac{10}{3})$ ***A1***

[2 marks]

(b) (i) **EITHER**

attempt to equate $h(t)$ to 2.5 ***(M1)***

$\dfrac{20}{2t+5}=2.5$

OR

attempt to substitute 2.5 in h^{-1} ***(M1)***

$\dfrac{20-5\times 2.5}{2\times 2.5}$

OR

graph of h, with an indication of the point $(t,2.5)$ ***(M1)***

$t=1.5$ (hours) ***A1***

(ii) It takes 1.5 hours for the water level to reach 2.5 metres. ***R1***

[3 marks]

(c) $t\geq 0$ ***A1***

Note: Accept $h^{-1}\geq 0$.

[1 mark]

Total [6 marks]

Q4.

(a) (i) -2 ***A1***

(ii) $0.667\left(0.66666..., \frac{2}{3}\right)$ ***A1***

Note: Award ***A1A0*** for answers given as coordinates $(-2, 6)$ and $(0.667, -3.48)$.
Accept answers which round to the correct 3 sf value (-2.00), e.g. -1.9999

[2 marks]

(b) $-2 < x < \frac{2}{3}$ ***A1***

Note: Award ***A1*** for correct inequalities and their endpoints.

[1 mark]

(c) (i) 3 ***A1***

(ii) $y + 3 = 3(x - 1)$ OR $y = 3x - 6$ ***A1***

[2 marks]

Total [5 marks]

Q5.

(a) midpoint of $[AB]$: $(4, 6.5)$ ***(A1)***

gradient of $[AB]$: $\frac{1}{2}$ ***(A1)***

gradient of perpendicular line: -2 ***(M1)***

Note: Award ***M1*** for gradient of perpendicular line. Allow follow through from their gradient of $[AB]$.

$y - 6.5 = -2(x - 4)$ OR $y = -2x + 14.5$ ***A1***

[4 marks]

(b) Option 3 ***A2***

[2 marks]

Note: Award ***A1A0*** if 2 options are selected and 1 of them is Option 3. Award ***A0A0*** in all other cases.

(c) attempt to find distance $(6, 4)$ to D or to draw a circle with radius 3 on the diagram ***M1***

$\sqrt{2^2 + 2^2} = \sqrt{8}, 2.82842...$

Yes (she is experiencing excellent coverage) ***A1***

EITHER

2.83 (km) < 3 km ***R1***

OR

$(6,4)$ is within a radius of 3 km from site D ***R1***

Note: Allow follow through for the ***R1*** from their distance. Award at most ***M0R1FTA0*** for comparing their distance with 3 km. Condone truncated 2 or 3 sf values for the ***R*** mark.
Do not award ***A1R0.***

continued

Question 5 continued.

Note: Allow the use of point B for candidates who assume the new towers have not yet been built.

attempt to find distance $(6, 4)$ to B or to draw a circle with radius 3 on the diagram ***M1***

$\sqrt{4^2 + 1^2} = \sqrt{17} = 4.12310...$

No (she is not experiencing excellent coverage) ***A1***

EITHER

4.12 (km) > 3 km ***R1***

OR

$(6,4)$ is not within a radius of 3 km from site B ***R1***

[3 marks]

Total [9 marks]

Q6.

(a) attempt to use the cosine rule formula ***(M1)***

$(\text{NV} =)\sqrt{20^2 + 25^2 - 2\times 20\times 25\cos 55.5^\circ}$ ***(A1)***

$= 21.4(\text{m})(21.4148...)$ ***A1***

[3 marks]

(b) **EITHER**

attempt to use the sine rule formula ***(M1)***

$\frac{\sin \text{P}\hat{\text{N}}\text{V}}{25} = \frac{\sin 55.5^\circ}{21.4148...}$ ***(A1)***

OR

attempt to use the cosine rule formula ***(M1)***

$\cos \text{P}\hat{\text{N}}\text{V} = \frac{20^2 + 21.4148...^2 - 25^2}{2\times 20\times 21.4148...}$ ***(A1)***

THEN

$\text{P}\hat{\text{N}}\text{V} = 74.2^\circ\left(74.1749...^\circ\right)$ ***A1***

[3 marks]

(c) recognition that shortest distance is perpendicular to NV ***(M1)***

(may be seen on diagram)

use of right-angled triangle or other valid method ***(M1)***

$\sin 74.1749...\times 20$ OR $\frac{1}{2}\times 20\times 25\times \sin 55.5^\circ \times \frac{2}{21.4148...}$

$= 19.2(\text{m})(19.2419...)$ ***A1***

Note: Accept 19.3 (m) from using their 3 sf value in $\frac{1}{2}\times 20\times 25\times \sin 55.5^\circ \times \frac{2}{21.4148...}$

[3 marks]

Total [9 marks]

Q7.

(a) attempt to substitute the given values in the function ***(M1)***

$(L =)10\log_{10}\left(\frac{10^{-5}}{10^{-12}}\right)$

$= 70(\text{dB})$ ***A1***

[2 marks]

(b) $185 = 10\log_{10}\left(\frac{I}{10^{-12}}\right)$ ***(A1)***

attempt to solve their logarithmic equation using graph, solver or analytically ***(M1)***

$I = 3160000(\text{Wm}^{-2})(3162277.66)$

$I = 3.16 \times 10^6 \ \ (3.16227... \times 10^6)$ ***A1***

Note*:* Award at most ***A1M1A0*** or ***A0M1A1FT*** for an incorrect answer written correctly in the required form.

[3 marks]

Total [5 marks]

Q8.

(a) H_1: satisfaction level and the type of service interaction are not independent. ***A1***

[1 mark]

(b) 4 ***A1***

[1 mark]

(c) $3.32\ (3.31906\ldots)$ ***A2***

Note: Award ***A1A0*** for a 2 sf answer of 3.3 as recognition of correct method.

[2 marks]

(d) (i) $3.319106\ldots < 9.488$ OR $0.506\ (\ 0.505917\ldots) > 0.05$ ***R1***

No, he isn't correct (insufficient evidence to reject H_0) ***A1***

Note: Accept a comparison in words (e.g. $\chi^2_{calc} < \chi^2_{crit}$ or '*p*-value < sig level') for the ***R*** mark only if their χ^2_{calc} value or *p*-value is seen. Do not award ***A1R0.***

(ii) insufficient evidence to say ''satisfaction level and the type of service interaction are not independent''. ***A1***

Note: Answer to part d (ii) follows through from their answer to part d(i).

[3 marks]

Total [7 marks]

Q9.

(a) evidence of integrating $\frac{\mathrm{d}P}{\mathrm{d}x}$ (***M1)***

$P = \int -10x + 460\,\mathrm{d}x$

$= -5x^2 + 460x(+c)$ ***A1A1***

Note: Award ***A1*** for each correct term. Omission of the constant c may be ignored at this stage.

evidence of substituting $x = 10$ and $P = 3300$ in their profit expression ***(M1)***

$P = -5x^2 + 460x - 800$ ***A1***

[5 marks]

(b) attempt at using definite integral with limits 25 and 50 OR attempt at finding the difference between $P(50)$ and $P(25)$ ***M1***

$\int_{25}^{50} -10x + 460\,\mathrm{d}x$ OR $P(50) - P(25)$

$= 2130(\mathrm{MUR})(2125)$ ***A1***

Note: Do not apply FT in part (b) if their final answer in part (a) is a constant, as it implies profit does not depend on x.

[2 marks]

Total [7 marks]

Q10.

(a) 4 ***A1***

[1 mark]

(b) identification of lower quartile as 24.28 ***(A1)***

$24.70 - 24.28$

0.42 (seconds) ***A1***

[2 marks]

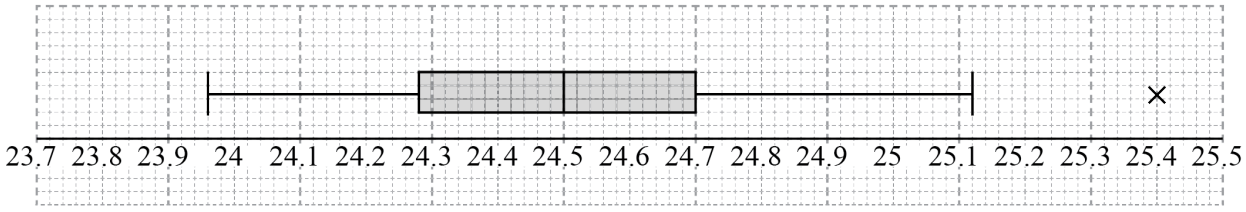
(c) (i) attempt to use correct formula to find boundaries for outliers ***(M1)***

$24.70 + 1.5 \times 0.42$ OR $24.28 - 1.5 \times 0.42$

25.33 and 23.65 ***A1***

only 25.4 is an outlier ***A1***

(ii)



A1

Note: Award the ***A1*** only if both whiskers and the outlier are correctly marked. Accept symbols other than a cross to represent the outlier. The whiskers should not be drawn through the box.

[4 marks]

Total [7 marks]

Q11.

(a) evidence of correct method ***(M1)***

$N = 300, I\% = 4.2, PV = \mp 50000, FV = 0, P/Y = 12, C/Y = 12$ OR 269.4711 seen

Note: Award ***M1*** for using the financial app on their GDC with at least 2 correct entries.

269.47(euros) ***A1***

Note: Award at most ***(M1)A0*** for -269.47. Accept 269.48.

[2 marks]

(b) (i) evidence of correct method $N = 96$ ***(M1)***

$N = 96,\ I\% = 4.2,\ PV = \mp 50000,\ PMT = \pm 269.47,\ P/Y = 12,\ C/Y = 12$

OR

$N = 96,\ I\% = 0.35,\ PV = \mp 50000,\ PMT = \pm 269.47,\ P/Y = 1,\ C/Y = 1$

Note: Award ***M1*** for using the financial app on their GDC with at least 2 correct entries.

$39,\ 243.42$ ***A1***

Note: Accept $39{,}243.29$ which results from the full calculator value for the payment in part (a). Accept $39{,}243.28$ which results from the use of 269.48.

Note: If two decimal place accuracy was penalised in part (a) do not penalise again.

(ii) **METHOD 1**

full payment $12 \times 25 \times 269.47 = 80{,}841.00$ ***(A1)***
actual payment $12 \times 8 \times 269.47 + 39243.42$ ***(M1)***

= $65,\ 112.54$ ***(A1)***

money saved = $15{,}700$ $(15{,}728.46)$ (euros) ***A1***

Note: Accept $15{,}728.59$ from using 269.47 from part (a) and $39{,}243.29$ from part (b)(i).
Accept $15{,}730.64$ from using 269.48 from part (a) and $39{,}243.28$ from part b(i).

continued

Question 11 continued

METHOD 2

if Sophie did not pay back the loan early her subsequent payments would be $269.47 \times 12 \times 17$ ***(M1)***

Note: Award ***M1*** for attempting to find the remaining amount to pay if loan not paid back.

$= 54971.88$ (euros) ***(A1)***

money saved is therefore
$54971.88 - 39243.42$ ***(M1)***

$= 15,700 (15,728.46)$ (euros) ***A1***

[6 marks]
Total [8 marks]

Q12.

(a) stratified (sampling) ***A1***

[1 mark]

(b) (i) $r = 0.854$ $(0.853899...)$ ***A2***

Note: Award ***(M1)A0*** for a truncated value $r = 0.853$ or incorrectly rounded value eg. $r = 0.85$.

(ii) it is valid (since $r > 0.8$) ***A1***

Note: Follow through from their value of r, for the final ***A1.***

[3 marks]

(c) $y = 0.266x + 2.40$ $(y = 0.265851...x + 2.39573...)$ ***A1***

Note: Accept 2.4.

[1 mark]

(d) substitution of 17.2 into their regression line ***(M1)***
$y = 0.265851... \times 17.2 + 2.39573...$
$= 6.97 (6.96837...)$ ***A1***

Note: Accept $6.98 (6.9752)$ from use of 3sf answers from part (c).

[2 marks]
Total [7 marks]