

Markscheme

May 2025

**Mathematics: applications and
interpretation**

Higher level

Paper 1

© International Baccalaureate Organization 2025

All rights reserved. No part of this product may be reproduced in any form or by any electronic or mechanical means, including information storage and retrieval systems, without the prior written permission from the IB. Additionally, the license tied with this product prohibits use of any selected files or extracts from this product. Use by third parties, including but not limited to publishers, private teachers, tutoring or study services, preparatory schools, vendors operating curriculum mapping services or teacher resource digital platforms and app developers, whether fee-covered or not, is prohibited and is a criminal offense.

More information on how to request written permission in the form of a license can be obtained from <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

© Organisation du Baccalauréat International 2025

Tous droits réservés. Aucune partie de ce produit ne peut être reproduite sous quelque forme ni par quelque moyen que ce soit, électronique ou mécanique, y compris des systèmes de stockage et de récupération d'informations, sans l'autorisation écrite préalable de l'IB. De plus, la licence associée à ce produit interdit toute utilisation de tout fichier ou extrait sélectionné dans ce produit. L'utilisation par des tiers, y compris, sans toutefois s'y limiter, des éditeurs, des professeurs particuliers, des services de tutorat ou d'aide aux études, des établissements de préparation à l'enseignement supérieur, des fournisseurs de services de planification des programmes d'études, des gestionnaires de plateformes pédagogiques en ligne, et des développeurs d'applications, moyennant paiement ou non, est interdite et constitue une infraction pénale.

Pour plus d'informations sur la procédure à suivre pour obtenir une autorisation écrite sous la forme d'une licence, rendez-vous à l'adresse <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

© Organización del Bachillerato Internacional, 2025

Todos los derechos reservados. No se podrá reproducir ninguna parte de este producto de ninguna forma ni por ningún medio electrónico o mecánico, incluidos los sistemas de almacenamiento y recuperación de información, sin la previa autorización por escrito del IB. Además, la licencia vinculada a este producto prohíbe el uso de todo archivo o fragmento seleccionado de este producto. El uso por parte de terceros —lo que incluye, a título enunciativo, editoriales, profesores particulares, servicios de apoyo académico o ayuda para el estudio, colegios preparatorios, desarrolladores de aplicaciones y entidades que presten servicios de planificación curricular u ofrezcan recursos para docentes mediante plataformas digitales—, ya sea incluido en tasas o no, está prohibido y constituye un delito.

En este enlace encontrará más información sobre cómo solicitar una autorización por escrito en forma de licencia: <https://ibo.org/become-an-ib-school/ib-publishing/licensing/applying-for-a-license/>.

Instructions to Examiners

Abbreviations

- M** Marks awarded for attempting to use a correct **Method**.
- A** Marks awarded for an **Answer** or for **Accuracy**; often dependent on preceding **M** marks.
- R** Marks awarded for clear **Reasoning**.
- AG** Answer given in the question and so no marks are awarded.
- FT** Follow through. The practice of awarding marks, despite candidate errors in previous parts, for their correct methods/answers using incorrect results.

Using the markscheme

1 General

Award marks using the annotations as noted in the markscheme *eg M1, A2*.

2 Method and Answer/Accuracy marks

- Do **not** automatically award full marks for a correct answer; all working **must** be checked, and marks awarded according to the markscheme.
- It is generally not possible to award **M0** followed by **A1**, as **A** mark(s) depend on the preceding **M** mark(s), if any.
- Where **M** and **A** marks are noted on the same line, *e.g. M1A1*, this usually means **M1** for an **attempt** to use an appropriate method (*e.g.* substitution into a formula) and **A1** for using the **correct** values.
- Where there are two or more **A** marks on the same line, they may be awarded independently; so if the first value is incorrect, but the next two are correct, award **A0A1A1**.
- Where the markscheme specifies **A3, M2** etc., do **not** split the marks, unless there is a note.
- The response to a “show that” question does not need to restate the **AG** line, unless a **Note** makes this explicit in the markscheme.
- Once a correct answer to a question or part question is seen, ignore further working even if this working is incorrect and/or suggests a misunderstanding of the question. This will encourage a uniform approach to marking, with less examiner discretion. Although some candidates may be advantaged for that specific question item, it is likely that these candidates will lose marks elsewhere too.
- An exception to the previous rule is when an incorrect answer from further working is used **in a subsequent part**. For example, when a correct exact value is followed by an incorrect decimal approximation in the first part and this approximation is then used in the second part. In this situation, award **FT** marks as appropriate but do not award the final **A1** in the first part.

Examples:

	Correct answer seen	Further working seen	Any FT issues?	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	No. Last part in question.	Award A1 for the final mark (condone the incorrect further working)
2.	$\frac{35}{72}$	0.468111... (incorrect decimal value)	Yes. Value is used in subsequent parts.	Award A0 for the final mark (and full FT is available in subsequent parts)

3 Implied marks

Implied marks appear in **brackets e.g. (M1)**, and can only be awarded if **correct** work is seen or implied by subsequent working/answer.

4 Follow through marks (only applied after an error is made)

Follow through (**FT**) marks are awarded where an incorrect answer from one **part** of a question is used correctly in **subsequent** part(s) (e.g. incorrect value from part (a) used in part (d) or incorrect value from part (c)(i) used in part (c)(ii)). Usually, to award **FT** marks, **there must be working present** and not just a final answer based on an incorrect answer to a previous part. However, if all the marks awarded in a subsequent part are for the answer or are implied, then **FT** marks should be awarded for *their* correct answer, even when working is not present.

For example: following an incorrect answer to part (a) that is used in subsequent parts, where the markscheme for the subsequent part is **(M1)A1**, it is possible to award full marks for *their* correct answer, **without working being seen**. For longer questions where all but the answer marks are implied this rule applies but may be overwritten by a **Note** in the Markscheme.

- Within a question part, once an **error** is made, no further **A** marks can be awarded for work which uses the error, but **M** marks may be awarded if appropriate.
- If the question becomes much simpler because of an error then use discretion to award fewer **FT** marks, by reflecting on what each mark is for and how that maps to the simplified version.
- If the error leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- The markscheme may use the word “their” in a description, to indicate that candidates may be using an incorrect value.
- If the candidate’s answer to the initial question clearly contradicts information given in the question, it is not appropriate to award any **FT** marks in the subsequent parts. This includes when candidates fail to complete a “show that” question correctly, and then in subsequent parts use their incorrect answer rather than the given value.
- Exceptions to these **FT** rules will be explicitly noted on the markscheme.
- If a candidate makes an error in one part but gets the correct answer(s) to subsequent part(s), award marks as appropriate, unless the command term was “Hence”.

5 Mis-read

If a candidate incorrectly copies values or information from the question, this is a mis-read (**MR**). A candidate should be penalized only once for a particular misread. Use the **MR** stamp to indicate that this has been a misread and do not award the first mark, even if this is an **M** mark, but award all others as appropriate.

- If the question becomes much simpler because of the **MR**, then use discretion to award fewer marks.
- If the **MR** leads to an inappropriate value (e.g. probability greater than 1, $\sin \theta = 1.5$, non-integer value where integer required), do not award the mark(s) for the final answer(s).
- Miscopying of candidates' own work does **not** constitute a misread, it is an error.
- If a candidate uses a correct answer, to a "show that" question, to a higher degree of accuracy than given in the question, this is NOT a misread and full marks may be scored in the subsequent part.
- **MR** can only be applied when work is seen. For calculator questions with no working and incorrect answers, examiners should **not** infer that values were read incorrectly.

6 Alternative methods

Candidates will sometimes use methods other than those in the markscheme. Unless the question specifies a method, other correct methods should be marked in line with the markscheme. If the command term is 'Hence' and not 'Hence or otherwise' then alternative methods are not permitted unless covered by a note in the mark scheme.

- Alternative methods for complete questions are indicated by **METHOD 1**, **METHOD 2**, etc.
- Alternative solutions for parts of questions are indicated by **EITHER . . . OR**.

7 Alternative forms

Unless the question specifies otherwise, **accept** equivalent forms.

- As this is an international examination, accept all alternative forms of **notation** for example 1.9 and 1,9 or 1000 and 1,000 and 1.000.
- Do not accept final answers written using calculator notation. However, **M** marks and intermediate **A** marks can be scored, when presented using calculator notation, provided the evidence clearly reflects the demand of the mark.
- In the markscheme, equivalent **numerical** and **algebraic** forms will generally be written in brackets immediately following the answer.
- In the markscheme, some **equivalent** answers will generally appear in brackets. Not all equivalent notations/answers/methods will be presented in the markscheme and examiners are asked to apply appropriate discretion to judge if the candidate work is equivalent.

8 Format and accuracy of answers

If the level of accuracy is specified in the question, a mark will be linked to giving the answer to the required accuracy. If the level of accuracy is not stated in the question, the general rule applies to final answers: *unless otherwise stated in the question all numerical answers must be given exactly or correct to three significant figures.*

Where values are used in subsequent parts, the markscheme will generally use the exact value, however candidates may also use the correct answer to 3 sf in subsequent parts. The markscheme will often explicitly include the subsequent values that come “*from the use of 3 sf values*”.

Simplification of final answers: Candidates are advised to give final answers using good mathematical form. In general, for an **A** mark to be awarded, arithmetic should be completed, and any values that lead to integers should be simplified; for example, $\sqrt{\frac{25}{4}}$ should be written as $\frac{5}{2}$. An exception to this is simplifying fractions, where lowest form is not required (although the numerator and the denominator must be integers); for example, $\frac{10}{4}$ may be left in this form or written as $\frac{5}{2}$.

However, $\frac{10}{5}$ should be written as 2, as it simplifies to an integer.

Algebraic expressions should be simplified by completing any operations such as addition and multiplication, e.g. $4e^{2x} \times e^{3x}$ should be simplified to $4e^{5x}$, and $4e^{2x} \times e^{3x} - e^{4x} \times e^x$ should be simplified to $3e^{5x}$. Unless specified in the question, expressions do not need to be factorized, nor do factorized expressions need to be expanded, so $x(x+1)$ and $x^2 + x$ are both acceptable.

Please note: intermediate **A** marks do NOT need to be simplified.

9 Calculators

A GDC is required for this paper, but if you see work that suggests a candidate has used any calculator not approved for IB DP examinations (eg CAS enabled devices), please follow the procedures for malpractice.

10. Presentation of candidate work

Crossed out work: If a candidate has drawn a line through work on their examination script, or in some other way crossed out their work, do not award any marks for that work unless an explicit note from the candidate indicates that they would like the work to be marked.

More than one solution: Where a candidate offers two or more different answers to the same question, an examiner should only mark the first response unless the candidate indicates otherwise. If the layout of the responses makes it difficult to judge, examiners should apply appropriate discretion to judge which is “first”.

Q1.

(a) attempt to use the cosine rule formula **(M1)**

$$(NV =) \sqrt{20^2 + 25^2 - 2 \times 20 \times 25 \cos 55.5^\circ} \quad \textbf{(A1)}$$

$$= 21.4(\text{m})(21.4148\dots) \quad \textbf{A1}$$

[3 marks]

(b) **EITHER**

attempt to use the sine rule formula **(M1)**

$$\frac{\sin \hat{PNV}}{25} = \frac{\sin 55.5^\circ}{21.4148\dots} \quad \textbf{(A1)}$$

OR

attempt to use the cosine rule formula **(M1)**

$$\cos \hat{PNV} = \frac{20^2 + 21.4148\dots^2 - 25^2}{2 \times 20 \times 21.4148\dots} \quad \textbf{(A1)}$$

THEN

$$\hat{PNV} = 74.2^\circ (74.1749\dots^\circ) \quad \textbf{A1}$$

[3 marks]

(c) recognition that shortest distance is perpendicular to NV **(M1)**

(may be seen on diagram)

use of right-angled triangle or other valid method **(M1)**

$$\sin 74.1749\dots \times 20 \quad \textbf{OR} \quad \frac{1}{2} \times 20 \times 25 \times \sin 55.5^\circ \times \frac{2}{21.4148\dots}$$

$$= 19.2(\text{m})(19.2419\dots) \quad \textbf{A1}$$

Note: Accept 19.3 (m) from using their 3 sf value in $\frac{1}{2} \times 20 \times 25 \times \sin 55.5^\circ \times \frac{2}{21.4148\dots}$

[3 marks]

Total [9 marks]

Q2.

(a) attempt to substitute the given values in the function **(M1)**

$$(L =) 10 \log_{10} \left(\frac{10^{-5}}{10^{-12}} \right)$$

$$= 70(\text{dB})$$

A1

[2 marks]

(b) $185 = 10 \log_{10} \left(\frac{I}{10^{-12}} \right)$ **(A1)**

attempt to solve their logarithmic equation using graph, solver or analytically **(M1)**

$$I = 3160000(\text{Wm}^{-2})(3162277.66)$$

$$I = 3.16 \times 10^6 \quad (3.16227... \times 10^6)$$

A1

Note: Award at most **A1M1A0** or **A0M1A1FT** for an incorrect answer written correctly in the required form.

[3 marks]

Total [5 marks]

Q3.

(a) H_1 : satisfaction level and the type of service interaction are not independent. **A1**

[1 mark]

(b) 4 **A1**

[1 mark]

(c) 3.32 (3.31906...) **A2**

Note: Award **A1A0** for a 2 sf answer of 3.3 as recognition of correct method.

[2 marks]

(d) (i) $3.319106... < 9.488$ OR $0.506 (0.505917...) > 0.05$ **R1**

No, he isn't correct (insufficient evidence to reject H_0) **A1**

Note: Accept a comparison in words (e.g. $\chi^2_{calc} < \chi^2_{crit}$ or 'p-value < sig level') for the **R** mark only if their χ^2_{calc} value or p-value is seen. Do not award **A1R0**.

(ii) insufficient evidence to say "satisfaction level and the type of service interaction are not independent". **A1**

Note: Answer to part d (ii) follows through from their answer to part d(i).

[3 marks]

Total [7 marks]

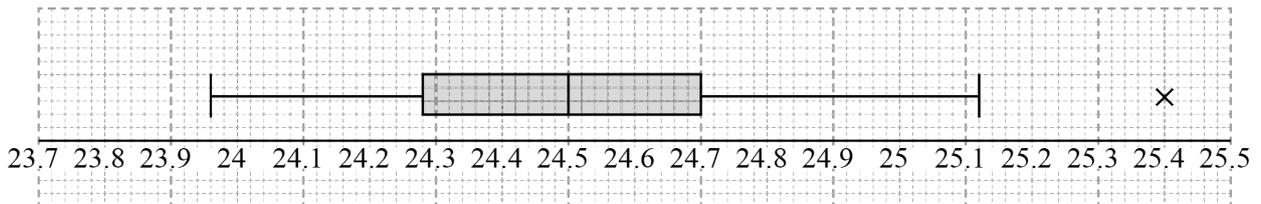
Q4.

- (a) 4 **A1**
[1 mark]
(b) identification of lower quartile as 24.28
24.70 – 24.28 **(A1)**

0.42 (seconds) **A1**
[2 marks]

- (c) (i) attempt to use correct formula to find boundaries for outliers **(M1)**
24.70 + 1.5 × 0.42 OR 24.28 – 1.5 × 0.42
25.33 and 23.65 **A1**
only 25.4 is an outlier **A1**

(ii)



A1

Note: Award the **A1** only if both whiskers and the outlier are correctly marked.
Accept symbols other than a cross to represent the outlier.
The whiskers should not be drawn through the box.

[4 marks]
Total [7 marks]

Q5.

- (a) evidence of correct method **(M1)**

$$N = 300, I\% = 4.2, PV = \mp 50000, FV = 0, P/Y = 12, C/Y = 12 \text{ OR } 269.4711 \text{ seen}$$

Note: Award **M1** for using the financial app on their GDC with at least 2 correct entries.

269.47(euros) **A1**

Note: Award at most **(M1)A0** for -269.47 . Accept 269.48.

[2 marks]

- (b) (i) evidence of correct method $N = 96$ **(M1)**

$$N = 96, I\% = 4.2, PV = \mp 50000, PMT = \pm 269.47, P/Y = 12, C/Y = 12$$

OR

$$N = 96, I\% = 0.35, PV = \mp 50000, PMT = \pm 269.47, P/Y = 1, C/Y = 1$$

Note: Award **M1** for using the financial app on their GDC with at least 2 correct entries.

39, 243.42 **A1**

Note: Accept 39,243.29 which results from the full calculator value for the payment in part (a). Accept 39,243.28 which results from the use of 269.48.

Note: If two decimal place accuracy was penalised in part (a) do not penalise again.

- (ii) **METHOD 1**

full payment $12 \times 25 \times 269.47 = 80,841.00$ **(A1)**

actual payment $12 \times 8 \times 269.47 + 39243.42$ **(M1)**

= 65, 112.54 **(A1)**

money saved = 15,700 (15,728.46) (euros) **A1**

Note: Accept 15,728.59 from using 269.47 from part (a) and 39,243.29 from part (b)(i).
Accept 15,730.64 from using 269.48 from part (a) and 39,243.28 from part b(i).

continued

Question 5 continued

METHOD 2

if Sophie did not pay back the loan early her subsequent payments would be $269.47 \times 12 \times 17$ **(M1)**

Note: Award **M1** for attempting to find the remaining amount to pay if loan not paid back.

= 54971.88 (euros) **(A1)**

money saved is therefore $54971.88 - 39243.42$ **(M1)**

= 15,700(15,728.46) (euros) **A1**

[6 marks]
Total [8 marks]

Q6

(a) use of formula for sum of an arithmetic sequence or first few terms seen **(M1)**

$$\frac{10}{2}(2 \times 6 + 9 \times 3) \text{ OR } 6 + 9 + 12 + 15 + \dots$$

sum of angles is 195° **(A1)**

$$p = \frac{195}{360} \left(0.542, \frac{13}{24}, 0.541666\dots \right) \quad \text{A1}$$

[3 marks]

(b) recognition of binomial distribution **(M1)**

$$n = 4, p = \frac{195}{360} \text{ OR } X \sim B\left(4, \frac{195}{360}\right) \quad \text{(A1)}$$

let X be the number of times the arrow lands in white

$$P(X \geq 3) = 0.377 \text{ (0.377450\dots)} \quad \text{A1}$$

Note: Accept 0.378 (0.377988...) from use of 0.542 from part (a).

[3 marks]
Total [6 marks]

Q7.

(a) stratified (sampling)

A1
[1 mark]

(b) (i) $r = 0.854$ (0.853899...)

A2

Note: Award **(M1)A0** for a truncated value $r = 0.853$ or incorrectly rounded value eg. $r = 0.85$.

(ii) it is valid (since $r > 0.8$)

A1

Note: Follow through from their value of r , for the final **A1**.

[3 marks]

(c) $y = 0.266x + 2.40$ ($y = 0.265851...x + 2.39573...$)

A1

Note: Accept 2.4.

(d) substitution of 17.2 into their regression line

[1 mark]
(M1)

$$y = 0.265851... \times 17.2 + 2.39573...$$

$$= 6.97(6.96837...)$$

A1

Note: Accept 6.98(6.9752) from use of 3sf answers from part (c).

[2 marks]

Total [7 marks]

Q8. EITHER

attempt to find matrix for compound transformation

(M1)

$$\begin{pmatrix} 3 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 1 & 3 \\ 1 & 0 \end{pmatrix}$$

(A1)

$$\begin{pmatrix} 1 & 3 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 4 \\ 7 \end{pmatrix}$$

(A1)

multiply by the inverse(s) or form two equations

(M1)

OR

$$\begin{pmatrix} 3 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} b_1 \\ b_2 \end{pmatrix} = \begin{pmatrix} 4 \\ 7 \end{pmatrix}$$

(A1)

multiply by the inverse or form two equations

(M1)

coordinates of B are $(-1, 7)$

(A1)

attempt to find coordinates for A by setting up matrix

(M1)

$$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix} = \begin{pmatrix} -1 \\ 7 \end{pmatrix}$$

THEN

$(7, -1)$

A1

Total [5 marks]

- Q9** (a) attempt to use product rule, two terms with one term correct (M1)
attempt to use the chain rule to find the derivative of $\sqrt{3x-2}$ (M1)

$$\frac{dy}{dx} = 4(3x-2)^{0.5} + 4x \times \frac{3}{2}(3x-2)^{-0.5} \quad \text{A1}$$

$$\left(= 4(3x-2)^{0.5} + 6x(3x-2)^{-0.5} \right) \left(= \frac{2(9x-4)}{\sqrt{3x-2}} \right)$$

[3 marks]

- (b) substitution of $x = 6$ into their $\frac{dy}{dx}$ (M1)

gradient of tangent = $(16 + 9 =) 25$ A1

Note: Follow through for this **A1** from their $\frac{dy}{dx}$.

at $(6, 96)$ tangent is

EITHER

$$y - 96 = 25(x - 6) \quad \text{A1}$$

OR

$$96 = 25 \times 6 + c \quad \text{A1}$$

Note: Do not allow follow through for this **A1**.

THEN

$$y = 25x - 54$$

AG

[3 marks]

Total [6 marks]

- Q10.** (a) (i) $F = \frac{k}{d^2}$ (A1)
 substitution of d and F into their equation (M1)
 $40000 = \frac{k}{7000^2}$
 $k = 1.96 \times 10^{12}$
 $F = \frac{1.96 \times 10^{12}}{d^2}$ A1
- (ii) $F = \frac{1.96 \times 10^{12}}{3500^2}$
 160000 (N) A1
[4 marks]
- (b) (i) C A1
 D A1

Note: Award at most **A1A0** if an additional incorrect answer is given.

- (ii) for C the gradient is $k = 1.96 \times 10^{12}$ A1
 for D the gradient is -2 A1
[4 marks]
Total [8 marks]

- Q11.** (a) C A1
[1 mark]
- (b) attempting to substitute values into the correct formulae (M1)
 $x_{n+1} = x_n + 0.1(3x_n - 2y_n)$, $y_{n+1} = y_n + 0.1(4x_n - y_n)$ (A1)
 $(t_{n+1} = t_n + 0.1)$
 any correct value for x_{n+1} and y_{n+1} for $n = 2, 3, \dots$ (A1)

n	t	x	y
0	5	1	0
1	5.1	1.3	0.4
2	5.2	1.61	0.88
3	5.3	1.917	1.436
4	5.4	2.2049	2.0592

$x = 2.45$ (2.45453...) A1

Note: Accept $x = 2.455$ from rounding to 4 sf.

$y = 2.74$ (2.73524...) A1
[5 marks]
Total [6 marks]

- Q12.** (a) (i) rejecting the null hypothesis when it is true **A1**
OR
rejecting the mean as 12.4 / min (124 / 10 mins) when it is true **A1**
- (ii) let X be the number of cars that arrive in 10 minutes
attempt to find $P(X \geq 131)$ **(M1)**
use of $Po(124)$ **(M1)**
 $P(X \geq 131) = 0.276$ (0.276397...) **A1**
[4 marks]
- (b) any valid reason **R1**
for example:
the arrival of cars are not independent (there might be a traffic light shortly before the intersection)
the rate of arrival is not uniform (some times of day might be busier than others)

Note: Do not accept "mean and variance are not the same".

[1 mark]
Total [5 marks]

- Q13.** (a) $\frac{dP}{dt} = 0.2(1 - P)$
 attempt to separate variables **M1**
 $\int \frac{1}{1 - P} dP = \int 0.2 dt$
 attempt to integrate left hand side by substitution or inspection. **(M1)**

Note: The **(M1)** may be awarded if their LHS is $\ln(1 - P)$ without the minus.

$$-\ln(1 - P) = 0.2t (+c) \quad \text{A1A1}$$

Note: Modulus sign not required as $0 \leq P < 1$.

EITHER

substitution of $P = 0$ when $t = 0$ **M1**

$$-\ln(1 - 0) = 0.2(0) + c \Rightarrow c = 0 \quad \text{A1}$$

eliminating the natural logarithm **M1**

$$1 - P = e^{-0.2t}$$

OR

eliminating the natural logarithm **M1**

$$1 - P = e^{-0.2t - c} \text{ or } 1 - P = Ae^{-0.2t}$$

substitution of $P = 0$ when $t = 0$ **M1**

$$1 = e^{-c} \Rightarrow c = 0 \text{ OR } 1 = A \quad \text{A1}$$

THEN

$$P = 1 - e^{-0.2t} \quad \text{AG}$$

[7 marks]

- (b) attempt to solve $0.9 = 1 - e^{-0.2t}$ **(M1)**

11.5 (days) (11.5129...)
A1

[2 marks]
Total [9 marks]

- Q14.** (a) $\begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = \begin{pmatrix} -20 \\ -9.8t \end{pmatrix}$ **A1A1**
[2 marks]
- (b) $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -20t + d \\ -4.9t^2 + 70 \end{pmatrix}$ **(A1)(A1)**
 recognition that package hits the ground when $-4.9t^2 + 70 = 0$ **(M1)**
 $t^2 = \frac{70}{4.9} \Rightarrow t = 3.77964\dots$ seconds **(A1)**
 attempt to solve $-20t + d = 0$ **(M1)**
 $d = 20 \times 3.7796\dots$
 distance $d = 75.6$ (75.5928...) (m) **A1**
[6 marks]
Total [8 marks]

- Q15.** (a) $\begin{pmatrix} p-1 & 1-q \\ 1-p & q-1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ or $\begin{pmatrix} p & 1-q \\ 1-p & q \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix}$ **(M1)**
- $(p-1)x + (1-q)y = 0$ (or equivalent) **(A1)**
- $\begin{pmatrix} 1-q \\ 1-p \end{pmatrix}$ (or any multiple) **A1**
[3 marks]
- (b) $\frac{1-q}{2-p-q}$ **A1A1**

Note: Award **A1** for numerator, **A1** for denominator.
 For an answer of $1 - q$ only, award **A0A0**.

- (c) $\frac{4}{11}(0.364, 0.363636\dots)$ **A1**
[1 mark]
Total [6 marks]

Q16. (a) $g(x) = 4 \cos\left(\frac{\pi}{8}(x+0.3)\right) - 0.2$ **A1A1**

Note: Accept $g(x) = f(x+0.3) - 0.2$

[2 marks]

(b) 3.57 (3.57262...) **A1**
[1 mark]

(c) (i) use of formula for volume in at least one integral **M1**

Note: In this formula condone one of:
missing or incorrect limits, absence of π , absence of dx for the **M1**.

subtracting two volumes **M1**

$$\frac{\pi}{2} \int_0^4 \left(4 \cos\left(\frac{\pi}{8}x\right)\right)^2 dx - \frac{\pi}{2} \int_0^{3.57262\dots} \left(4 \cos\left(\frac{\pi}{8}(x+0.3)\right) - 0.2\right)^2 dx$$
A1A1

Note: Award **A1** for each completely correct expression (including the dx).
Award **A1A0** for everything correct except not dividing by two.

(ii) $\frac{\pi}{2}(32 - 23.7729\dots)$
12.9 cm³ (12.9229...) **A1**

Note: Do not award **A1FT** follow through for this part.

[5 marks]
Total [8 marks]